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# Population of $^{13}\text{Be}$ in a Nucleon Exchange Reaction

## Abstract

The neutron-unbound nucleus  $^{13}\text{Be}$  was populated with a nucleon exchange reaction from a 71 MeV/u secondary  $^{13}\text{B}$  beam. The decay-energy spectrum was reconstructed using invariant mass spectroscopy based on  $^{12}\text{Be}$  fragments in coincidence with neutrons. The data could be described with an s-wave resonance at  $E_r=0.73(9)\text{MeV}$  with a width of  $\Gamma_r=1.98(34)\text{MeV}$  and a d-wave resonance at  $E_r=2.56(13)\text{MeV}$  with a width of  $\Gamma_r=2.29(73)\text{MeV}$ . The observed spectral shape is consistent with previous one-proton removal reaction measurements from  $^{14}\text{B}$ .

## Disciplines

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## Population of $^{13}\text{Be}$ in a nucleon exchange reaction

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The neutron-unbound nucleus  $^{13}\text{Be}$  was populated with a nucleon exchange reaction from a 71 MeV/u secondary  $^{13}\text{B}$  beam. The decay-energy spectrum was reconstructed using invariant mass spectroscopy based on  $^{12}\text{Be}$  fragments in coincidence with neutrons. The data could be described with an  $s$ -wave resonance at  $E_r = 0.73(9)$  MeV with a width of  $\Gamma_r = 1.98(34)$  MeV and a  $d$ -wave resonance at  $E_r = 2.56(13)$  MeV with a width of  $\Gamma_r = 2.29(73)$  MeV. The observed spectral shape is consistent with previous one-proton removal reaction measurements from  $^{14}\text{B}$ .

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### I. INTRODUCTION

Recent experimental investigations of the level structure of the neutron-unbound nucleus  $^{13}\text{Be}$  agree about the overall strength distribution of the excitation energy spectrum [1–6], but there is no consensus on its interpretation. While there seems to be general agreement about the presence of a broad  $s$ -wave resonance below 1 MeV and a  $d$ -wave resonance at 2 MeV, the composition of the observed peak around 500 keV, as well as the decay paths of the  $d$ -wave resonance, are still being discussed. Earlier reports of a narrow low-lying  $s$ -wave state [7,8] have been attributed to a sequential decay from the first excited  $2^+$  state in  $^{14}\text{Be}$  to  $^{12}\text{Be}$  [3,6,9].

In 2010, Kondo *et al.* [3] reported a low-lying  $p$ -wave resonance at 510(10) keV populated by a one-neutron removal reaction from  $^{14}\text{Be}$  at 69 MeV/u. However, a recent analysis of these data, as well as a new measurement at a higher beam energy on a hydrogen target (304 MeV/u), preferred an interpretation which fits the  $\sim 500$  keV peak with only two interfering broad  $s$ -wave resonances [4,5]. Moreover, the presence of additional  $p$ - or  $d$ -wave strength could not be ruled out, indicating that an  $\ell \neq 0$  resonance around 1 MeV might exist [5]. The fits in both papers included a significant decay branch of the  $d_{5/2}$  state to the first excited  $2^+$  state in  $^{12}\text{Be}$ .

While neutron-removal reactions are expected to populate positive- as well as negative-parity states, proton-removal reactions should be more selective and populate only positive-parity states. Randisi *et al.* [6] measured the decay-energy

spectrum of  $^{13}\text{Be}$  following the one-proton removal reaction from  $^{14}\text{B}$  at 35 MeV/u and argued that the  $\sim 500$  keV peak consists of an  $s$ -wave resonance as well as a low-lying  $d$ -wave resonance. In addition, Randisi *et al.* searched for the decay of the  $d_{5/2}$  resonance at 2 MeV to the first excited  $2^+$  state in  $^{12}\text{Be}$  by measuring the  $\gamma$  rays from this state in coincidence. No significant branch of this decay mode was observed.

In the present work, the nucleon exchange reaction ( $-1p + 1n$ ) from  $^{13}\text{B}$  was used to populate states in  $^{13}\text{Be}$ . Similar to the proton-removal reaction it is expected to only populate positive-parity states. This type of reaction has been shown to have sizable cross sections at intermediate beam energies. For example, the one-proton removal–one-neutron addition ( $-1p + 1n$ ) reaction has been utilized with stable ( $^{48}\text{Ca}$ ) as well as radioactive ( $^{48}\text{K}$  and  $^{46}\text{Cl}$ ) beams to explore the structures of  $^{48}\text{K}$ ,  $^{48}\text{Ar}$ , and  $^{46}\text{S}$  [10]. The inclusive cross sections were 0.13(1) and 0.057(6) mb for the  $^9\text{Be}(^{48}\text{K}, ^{48}\text{Ar})$  and  $^9\text{Be}(^{46}\text{Cl}, ^{46}\text{S})$ , respectively. This ( $-1p + 1n$ ) reaction was also used for the first time to measure neutron unbound states in the study of  $^{26}\text{F}$  populated from a 86 MeV/u  $^{26}\text{Ne}$  beam [11].

### II. EXPERIMENTAL SETUP

The experiment was performed at the National Superconducting Cyclotron Laboratory at Michigan State University. A 120 MeV/u  $^{18}\text{O}$  primary beam from the Coupled Cyclotron Facility bombarded a 2.5 g cm<sup>2</sup>  $^9\text{Be}$  production target. The A1900 fragment separator was used to separate and select the  $^{13}\text{B}$  secondary beam. The final energy of the beam was 71 MeV/u, with an intensity of approximately  $8 \times 10^5$  particles per second and a purity of 96%. The  $^{13}\text{B}$  beam impinged upon a 51 mg cm<sup>2</sup>  $^9\text{Be}$  target where  $^{13}\text{Be}$  was

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produced in a nucleon exchange reaction and immediately decayed into  $^{12}\text{Be} + n$ .

The  $^{12}\text{Be}$  reaction products were deflected by a large-gap sweeper magnet [12] and identified from energy-loss and time-of-flight measurements. The  $^{12}\text{Be}$  energy and momentum vectors were reconstructed from position information and a transformation matrix based on the magnetic-field map using the program COSY INFINITY [13]. Coincident neutrons were measured with the Modular Neutron Array (MoNA) [14,15] and the Large-Area Multi-Institutional Scintillator Array (LISA). The energy and momentum vectors of the neutrons were determined from the positions of the neutron interactions in the arrays and the time-of-flight between the arrays and a scintillator located upstream near the target. The nucleon exchange data were recorded simultaneously with the data for the one-proton-removal reaction populating unbound states in  $^{12}\text{Be}$ . These results have been published recently in Ref. [16] where further details of the experimental setup and analysis can be found.

### III. DATA ANALYSIS

The decay-energy spectrum of  $^{13}\text{Be}$  was reconstructed by the invariant-mass method and is shown in Figs. 1 and 2. The spectrum shows the same general features as the previous measurements with a strong peak around 500 keV and an additional structure at about 2 MeV. The energy-dependent resolution (blue-dotted line) and the overall efficiency (red solid line) are shown in the insert of Fig. 1.

To interpret the measured decay-energy spectrum, Monte Carlo simulations were performed with the incoming beam characteristics, reaction mechanism, and detector resolutions taken into account. The neutron interactions within MoNA-LISA were simulated with GEANT4 [17,18] using the MENATE\_R package [19] as described in Ref. [20]. Resonances were parametrized using energy-dependent Breit-Wigner line shapes [16].

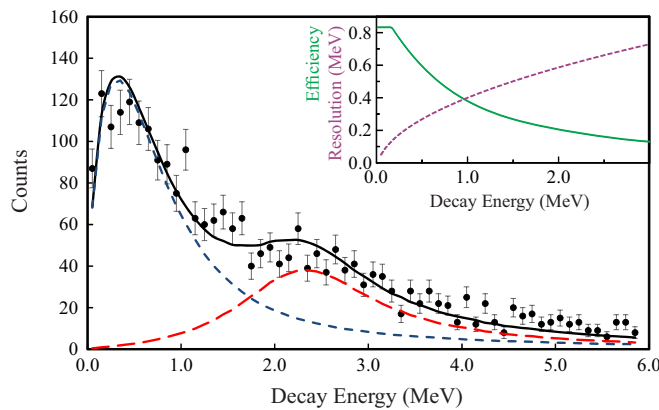


FIG. 1. (Color online) Decay-energy spectrum of  $^{13}\text{Be}$  fit with two components. The solid black line is the sum of simulated decay-energy spectra from an  $s$ -wave resonance (short-dashed blue line) and a  $d$ -wave resonance (long-dashed red line) with parameters listed in the text. The insert shows the energy-dependent resolution (dotted purple line) and the overall efficiency (solid green line).

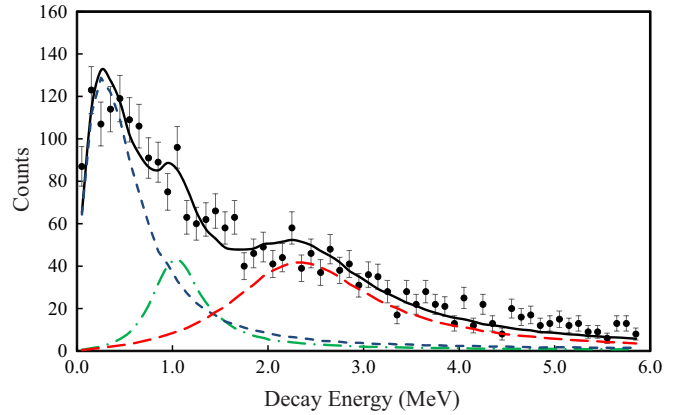


FIG. 2. (Color online) Decay-energy spectrum of  $^{13}\text{Be}$  fit with three components. The solid black line is the sum of simulated decay-energy spectra from an  $s$ -wave resonance (short-dashed blue line) and two  $d$ -wave resonances (long-dashed red line and dot-dashed green line) with parameters listed in the text.

The present nucleon exchange reaction is expected to populate the same positive-parity states that were populated in the one-proton-removal reaction. In that case, the valence neutron configuration of the  $^{14}\text{B}$  projectile is dominated by  $\nu 2s_{1/2}$  and  $\nu 1d_{5/2}$  components, and states with the same configurations are expected to be populated in  $^{13}\text{Be}$  by proton removal [6]. The ground state of  $^{13}\text{B}$  has spin and parity of  $3/2^-$  dominated by a  $(\pi 1p_{3/2})^3$  proton configuration and a closed  $sp$  shell neutron configuration. Removing the odd proton from  $^{13}\text{B}$  is similar to the proton removal from  $^{14}\text{B}$  while the added extra odd neutron will populate states in the open  $sd$  shell.

Randisi *et al.* were able to fit their data from the proton-removal reaction based on selectivity arguments with only two components, an  $s$ -wave resonance at  $E_r = 0.70(11)$  MeV with a width of  $\Gamma_r = 1.70(22)$  MeV and a  $d$ -wave resonance at  $E_r = 2.40(14)$  MeV with a width of  $\Gamma_r = 0.70(32)$  MeV [6]. The best fit to the decay-energy spectrum from the present nucleon exchange reactions is shown in Fig. 1 with an  $s$ -wave resonance at  $E_r = 0.73(9)$  MeV with a width of  $\Gamma_r = 1.98(34)$  MeV and a  $d$ -wave resonance at  $E_r = 2.56(13)$  MeV with a width of  $\Gamma_r = 2.29(73)$  MeV. Overall these parameters agree with the results from Randisi *et al.* with only the width of the  $d$ -wave resonance being somewhat larger.

The overall cross section for populating  $^{13}\text{Be}$  with the  $(-1p + 1n)$  reaction was extracted to be  $0.30(15)$  mb which is about an order of magnitude smaller than one-proton-removal reactions on neutron-rich  $p$ -shell nuclei. Kryger *et al.* reported a cross section of  $2.46(3)$  mb for the proton removal from  $^{16}\text{C}$  to  $^{15}\text{B}$  [21] and Lecouey *et al.* measured  $6.5(15)$  mb for the proton-removal reaction from  $^{17}\text{C}$  to  $^{16}\text{B}$  [22].

The cross section is somewhat larger than the cross section of  $0.1$  mb estimated for the charge-exchange reaction based on distorted-wave Born approximation (DWBA) calculations using the code FOLD [23]. Transition densities that were input to FOLD were calculated using the shell-model code OXBASH [24]. The CKII interaction [25] was used in the  $p$ -shell-model space to calculate the transition densities for the

TABLE I. Resonance parameters for the three-component fits. For each state with the proposed spin and parity ( $J^\pi$ ) shown, the resonance energy ( $E_r$ ), resonance width ( $\Gamma_r$ ), and population relative to the  $1/2^+$  state ( $I/I_{1/2^+}$ ) are listed for the proton-removal reaction of Randisi *et al.* ( $-1p$ ) [6] as well as the present nucleon exchange reaction ( $-1p + 1n$ ).

$J^\pi$	Randisi <i>et al.</i> [6] ( $-1p$ )			Present work ( $-1p + 1n$ )		
	$E_r$	$\Gamma_r$	$I/I_{1/2^+}$	$E_r$	$\Gamma_r$	$I/I_{1/2^+}$
$1/2^+$	$0.40 \pm 0.03$	$0.80^{+0.18}_{-0.12}$	1.00	$0.40^a$	$0.80^a$	1.00
$5/2_1^+$	$0.85^{+0.15}_{-0.11}$	$0.30^{+0.34}_{-0.15}$	$0.40 \pm 0.07$	$1.05 \pm 0.10$	$0.50 \pm 0.20$	$0.63 \pm 0.15$
$5/2_2^+$	$2.35 \pm 0.14$	$1.50 \pm 0.40$	$0.80 \pm 0.09$	$2.56 \pm 0.13^b$	$2.29 \pm 0.73^b$	$3.88 \pm 0.50$

<sup>a</sup>Fixed value from Randisi *et al.* [6].

<sup>b</sup>Value taken from two-parameter fit.

$^9\text{Be}$ – $^9\text{B}$  system, and the WBP interaction [26] was used in the *spstdpf*-shell-model space to calculate the transition densities for the  $^{13}\text{B}$ – $^{13}\text{Be}$  system. The effective nucleon-nucleon interaction of Ref. [27] was double folded over the transition densities to produce form factors. Optical-model potential parameters were taken from Ref. [28].

Guided by  $(0-3)\hbar\omega$  shell-model calculations Randisi *et al.* analyzed their data by introducing a second lower-lying  $d$ -wave resonance [6]. The resonance energies and widths for this analysis are listed in Table I together with the parameters used to fit the present data as shown in Fig. 2. A completely unconstrained three-resonance fit resulted in degenerate values for the lower two resonances. Thus the values for the  $s$ -wave resonance were constrained to the value of Randisi *et al.* ( $E_r = 0.40$  MeV,  $\Gamma_r = 0.80$  MeV) and the parameters for the second  $d$ -wave resonance were kept at the value extracted from the two-parameter fit ( $E_r = 2.56$  MeV,  $\Gamma_r = 2.29$  MeV). The resonance energy and width of the first  $d$ -wave resonance as well as strength of all three components were varied. Figure 2 shows that the nucleon exchange data can be well described with parameters similar to the one-proton-removal reaction.

Table I also includes the ratios of the  $d$ -wave resonances relative to the  $s$ -wave resonance for the two reactions. The relative intensities in the proton-removal reaction are governed by the ground-state configuration of  $^{14}\text{B}$  where the spectroscopic factors for populating the  $1/2^+$ ,  $5/2_1^+$ , and  $5/2_2^+$  were calculated within the WBP shell model to be 0.41, 0.13, and 0.43, respectively, in good agreement with the data [6]. The  $1/2^+$  and  $5/2_2^+$  states are dominated by single-particle configurations, whereas the  $5/2_1^+$  has  $2\hbar\omega$   $^{10}\text{Be} \otimes (\nu 2s 1d)^3$  parentage.

The intensity of the low-lying  $d$ -wave resonance in the nucleon exchange reaction is slightly larger than the intensity extracted from the proton-removal reaction, while the intensity of the second  $d$ -wave resonance is significantly larger. These ratios do not have to be the same for the two different reactions. For example, in addition to the two  $5/2^+$  states, the  $(0-3)\hbar\omega$  shell-model calculations also predict a low-lying  $3/2^+$  state. The spectroscopic factor of this state for proton removal from  $^{14}\text{B}$  is zero, so it is not expected to be observed in the data

of Randisi *et al.* [6]. It could, however, be populated in the present reaction which would reduce the strengths of the two  $d$ -wave resonances relative to the low-lying  $s$ -wave resonance. It should be mentioned that the low-lying  $3/2^+$  and  $5/2^+$  states predicted by the  $(0-3)\hbar\omega$  shell-model calculations using the WBP interaction [6] are not present in the simplified scheme by Fortune [29]. This discrepancy has recently been reiterated and is not fully understood [30].

Finally, the present data show no evidence of any low-energy decay from the second  $d_{5/2}$  to the first excited  $2^+$  state in  $^{12}\text{Be}$  as was suggested by Aksyutina *et al.* [5]. Simulations including such a decay branch resulted in an upper limit of less than 10%. This finding is consistent with results by Randisi *et al.* who extracted a branching ratio of 5(2)% [6].

#### IV. SUMMARY AND CONCLUSION

In conclusion, the  $^{13}\text{B}(-1p + 1n)$  nucleon exchange reaction was used to populate the neutron-unbound nucleus  $^{13}\text{Be}$ . The decay-energy spectrum can be described with resonance parameters similar to previously reported values for the proton-removal reaction from  $^{14}\text{B}$ . In general nucleon exchange reactions offer an alternative reaction mechanism to selectively populate states in neutron-rich nuclei when the nucleus of interest cannot be populated by single-proton (i.e.,  $^{15}\text{Be}$ ,  $^{20}\text{B}$ , or  $^{24}\text{N}$ ) or even two-proton ( $^{23}\text{C}$ ) removal reactions.

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