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# Neutron-Unbound Excited States of $^{23}\text{N}$

## Abstract

Neutron unbound states in  $^{23}\text{N}$  were populated via proton knockout from an 83.4 MeV/nucleon  $^{24}\text{O}$  beam on a liquid deuterium target. The two-body decay energy displays two peaks at  $E_1 \sim 100\text{keV}$  and  $E_2 \sim 1\text{MeV}$  with respect to the neutron separation energy. The data are consistent with shell model calculations predicting resonances at excitation energies of  $\sim 3.6\text{MeV}$  and  $\sim 4.5\text{MeV}$ . The selectivity of the reaction implies that these states correspond to the first and second  $3/2^-$  states. The energy of the first state is about 1.3 MeV lower than the first excited  $2^+$  in  $^{24}\text{O}$ . This decrease is largely due to coupling with the  $\pi p-13/2$  hole along with a small reduction of the  $N=16$  shell gap in  $^{23}\text{N}$ .

## Keywords

Neutron states, proton knockout, neutron separation energy, nuclear structure, nuclear decays, unstable nuclei, radioactive beams

## Disciplines

Atomic, Molecular and Optical Physics | Nuclear | Quantum Physics

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**Neutron-unbound excited states of  $^{23}\text{N}$** 

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Neutron unbound states in  $^{23}\text{N}$  were populated via proton knockout from an 83.4 MeV/nucleon  $^{24}\text{O}$  beam on a liquid deuterium target. The two-body decay energy displays two peaks at  $E_1 \sim 100$  keV and  $E_2 \sim 1$  MeV with respect to the neutron separation energy. The data are consistent with shell model calculations predicting resonances at excitation energies of  $\sim 3.6$  MeV and  $\sim 4.5$  MeV. The selectivity of the reaction implies that these states correspond to the first and second  $3/2^-$  states. The energy of the first state is about 1.3 MeV lower than the first excited  $2^+$  in  $^{24}\text{O}$ . This decrease is largely due to coupling with the  $\pi p_{3/2}^{-1}$  hole along with a small reduction of the  $N = 16$  shell gap in  $^{23}\text{N}$ .

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**I. INTRODUCTION**

Spectroscopy of nuclei with extreme  $N/Z$  ratios can provide valuable insight into nuclear structure. Due to shifts in the single particle energies of exotic nuclei, classical shell closures can disappear while new shell gaps appear [1,2]. A well-known example of this is the “island of inversion,” located around  $A \sim 32$ , where a quenching of the  $N = 20$  shell gap results in nuclei with ground states occupying the  $pf$  shell instead of the  $sd$  shell [3]. In the oxygen isotopes, there is substantial evidence for the breakdown of the  $N = 20$  shell gap, and the appearance of  $N = 16$  as a magic number [4–7]. This shift has been attributed to the tensor component of the  $NN$  interaction [8,9] as well as three-body forces [10].

As one moves down the  $N = 16$  isotones, the removal of protons from the  $\pi 0d_{5/2}$  orbital enables the  $\nu 0d_{3/2}$  orbital to move higher in excitation resulting in a large energy difference between the  $\nu 1s_{1/2}$  and  $\nu 0d_{3/2}$  orbits in oxygen [2]. At present, there are no reports of bound- or unbound-excited states in the lighter isotones  $^{23}\text{N}$  and  $^{22}\text{C}$ . The measurement of these excited states can provide a better understanding of the changing shell structure in this region of the nuclear chart by extending our knowledge of the  $N = 16$  gap into the proton  $p$  shell. In this article, we present first experimental information on neutron-unbound excited states in  $^{23}\text{N}$  populated via proton-knockout from  $^{24}\text{O}$ .

**II. EXPERIMENTAL METHOD**

The experiment was carried out at the National Superconducting Cyclotron Laboratory (NSCL) where a 140 MeV/nucleon  $^{48}\text{Ca}$  beam impinged upon a  $^9\text{Be}$  target with a thickness of 1363 mg/cm<sup>2</sup> to produce an  $^{24}\text{O}$  beam at 83.4 MeV/nucleon. The A1900 fragment separator was used to select  $^{24}\text{O}$  from the other fragmentation products, and the remaining beam contaminants were removed by time-of-flight in the off-line analysis. The  $^{24}\text{O}$  beam proceeded to the experimental area where it impinged on the Ursinus College Liquid Hydrogen Target, filled with liquid deuterium ( $\text{LD}_2$ ). Based on the design of Ryuto *et al.* [11], the  $\text{LD}_2$  target is cylindrical with a diameter of 38 mm, a length of 30 mm, and is sealed with 125  $\mu\text{m}$ -thick Kapton foils on each side.

A one-proton removal reaction from the  $^{24}\text{O}$  beam created  $^{23}\text{N}$  in an excited state above the neutron separation energy  $S_n$ , which promptly decayed to  $^{22}\text{N}$ . The resulting charged fragments were then swept 43.3° by a 4-Tm superconducting sweeper magnet [12] into a collection of position- and energy-sensitive charged-particle detectors.

Element identification was achieved via a  $\Delta E$  vs. time-of-flight measurement, and isotope identification was obtained through correlations in the time-of-flight, dispersive position, and dispersive angle following the sweeper magnet. Additional information on this procedure can be found in Ref. [13]. The position and momentum of the charged fragments at the target were reconstructed using an inverse transformation matrix, obtained from the program COSY INFINITY [14,15].

The neutrons emitted in the decay of  $^{23}\text{N}$  traveled undisturbed by the magnetic field towards the Modular Neutron Array (MoNA) [16] and the Large-area multi-Institutional

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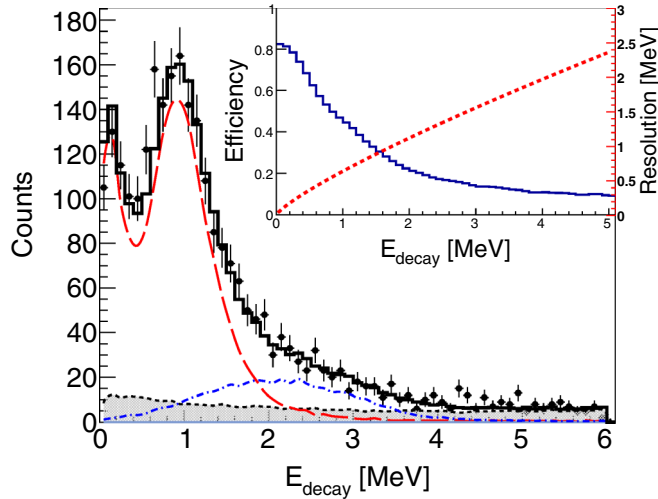


FIG. 1. Two-body decay energy for  $^{22}\text{N} + 1n$ . The best fit includes two-channel Breit-Wigners resulting from two states at 1.1 MeV (dashed-red line) and 2.4 MeV (dot-dashed-blue line). Background contributions are in shaded gray. The efficiency and resolution are shown in the inset as the blue histogram (left scale) and red-dashed line (right scale), respectively.

Scintillator Array (LISA). MoNA and LISA each consist of 144 bars of plastic scintillator with photomultiplier tubes on both ends and provide a measurement of neutron time-of-flight and position. Additional details on the experimental setup can be found in Refs. [17,18]. MoNA, LISA, and the sweeper provide a full kinematic measurement of the neutrons and charged particles emitted in the decay of  $^{23}\text{N}$ .

### III. ANALYSIS

The two-body decay energy is defined as

$$E_{\text{decay}} = M^* - M_{^{22}\text{N}} - m_n,$$

where  $M^*$  is the invariant mass of the decaying system,  $M_{^{22}\text{N}}$  the mass of  $^{22}\text{N}$ , and  $m_n$  the neutron mass. The decay energy,  $E_{\text{decay}}$ , corresponds to the excitation energy in  $^{23}\text{N}$  above the neutron emission threshold. The invariant mass of the two-body system is obtained from the experimentally measured four-momenta of  $^{22}\text{N}$  and the first time-ordered interaction in MoNA-LISA. To remove interactions from background  $\gamma$  rays, a time-of-flight gate on prompt neutrons in coincidence with  $^{22}\text{N}$  fragments was applied. The observed two-body decay energy for  $^{23}\text{N}$  is shown in Fig. 1, and displays two prominent peaks at  $E_1 \sim 100$  keV and  $E_2 \sim 1$  MeV. The efficiency and resolution of MoNA-LISA for the present setup are shown as a function of the decay energy in the inset.

A Monte Carlo simulation was used to model the decay of  $^{23}\text{N}$ . The simulation includes the beam characteristics, the reaction mechanism, and subsequent decay. The efficiency, resolution, and acceptance of the charged particle detectors, along with the response of MoNA-LISA, are fully incorporated into the simulation. Therefore the results of the simulation are directly comparable to the experimental spectra. The neutron interactions in MoNA-LISA were modeled with

GEANT4 [19] and MENATE\_R [20]. A modification was made to the  $^{12}\text{C}(n,np)^{11}\text{B}$  inelastic cross section within MENATE\_R to better agree with previous measurement [21] at  $T_n = 90$  MeV. No qualitative change was observed in the shape of the simulated one-neutron decay energy spectrum when the inelastic cross sections for neutrons on carbon were increased or decreased by an order of magnitude in MENATE\_R.

The input decay energy line shape was an energy dependent Breit-Wigner of the form

$$\sigma_l(E) \sim \frac{\Gamma_l}{(E_0 - E)^2 + \frac{1}{4}(\Gamma_l^2)},$$

where  $E_0$  is the position of the peak and  $\Gamma_l$  the energy-dependent width. Given that  $^{22}\text{N}$  has two bound excited states [22], it is possible for the neutron decay to branch to multiple final states. To model this, the two-channel form of the Breit-Wigner was used with a common normalization:

$$\sigma_{\text{tot}}(E) \sim \sigma_1(E; E_1) + \sigma_2(E; E_2),$$

where  $E_i$  is the energy of each branch, and the width in the numerator  $\Gamma_l$  becomes the partial-width  $\Gamma_i$ . The total widths  $\Gamma_i^T$  replace the width in the denominator and are given by the expressions

$$\Gamma_1^T = \Gamma_1(E) + \Gamma_2(E - E_{12}),$$

$$\Gamma_2^T = \Gamma_1(E + E_{12}) + \Gamma_2(E),$$

where  $E_{12} = E_1 - E_2$  is the energy difference between the channels, with  $E_1$  denoting the higher-energy channel. For simplicity, the shift functions have been neglected.

While it is possible for higher-lying states to be present at  $E_{\text{decay}} > 3$  MeV, they are not resolved in the data and treated as background. Nonresonant contributions were modeled with a Gaussian decay distribution with a central energy of  $E_{\text{decay}} = 10$  MeV and a width of  $\sigma = 5$  MeV. This choice of line-shape reproduces the relative velocity between the fragment and neutron well and has been used to describe nonresonant contributions in the decay of  $^{24}\text{O}$ , populated by knockout from  $^{26}\text{F}$  [4].

The measured decay energy can be related to the excitation energy of  $^{23}\text{N}$  by  $E^* = E_{\text{decay}} + S_n$ , where  $S_n$  was calculated using the mass excesses from Gaudefroy *et al.* [23]. Their values of  $\Delta M_{^{23}\text{N}} = 36.72(0.28)$  MeV and  $\Delta M_{^{22}\text{N}} = 31.11(0.26)$  MeV result in a one neutron separation energy of  $S_n = 2.46(0.38)$  MeV. This separation energy is about 700 keV higher than what is obtained using the masses in the 2012 AME [24]. The two-neutron separation energy is  $S_{2n} = 4.67(0.30)$  MeV.

Using the mass excesses measured by Gaudefroy *et al.* [23], theoretical predictions for the excited states of  $^{23}\text{N}$  are shown in Fig. 2 with various interactions based on Ref. [25] including the WBP, WBT, WBTM, and WBM Hamiltonians in addition to the continuum shell model (CSM) [26]. The WBTM and WBM interactions contain a 12.5% and 25% reduction of the neutron-neutron interaction strength in the  $sd$  space. In the lighter nitrogen isotopes, a 12.5% reduction was necessary to reproduce the low-lying levels [22,27], while a 25% reduction was needed for the heavier carbon nuclei [22]. Proton excitations were limited to the  $p$  shell, while neutron

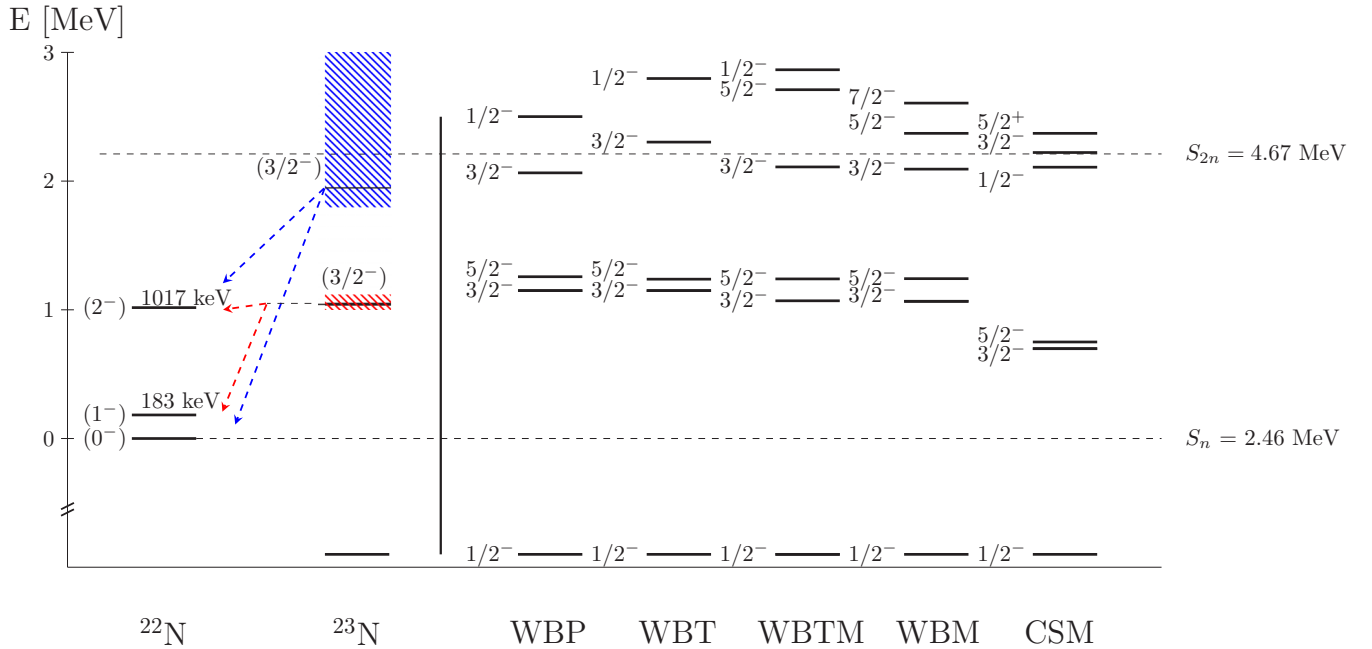


FIG. 2. A possible level ordering in  $^{23}\text{N}$  consistent with the observed spectrum. The arrows indicate transitions from the first- and second-excited  $3/2^-$  state in  $^{23}\text{N}$  to various states in  $^{22}\text{N}$ . The hatched areas indicate the experimental uncertainty given the assumptions discussed in the text. The colors correspond to the fit in Fig. 1. The branching from the  $3/2^-$  states to the various excited states of  $^{22}\text{N}$  cannot be resolved without  $\gamma$  detection. Shell model calculations for  $^{23}\text{N}$  are shown for comparison on the right.

excitations were restricted to the  $sd$  shell. These calculations predict several excited states with spin-parity  $1/2^-$ ,  $3/2^-$ , and  $5/2^-$  in the vicinity of 3–5 MeV. Due to the selective nature of the proton removal reaction, it is not likely to populate a  $5/2^-$  state in  $^{23}\text{N}$  from  $^{24}\text{O}$ . A  $5/2^-$  state in  $^{23}\text{N}$  can be made by coupling of the  $p_{1/2}$  proton hole to the  $2^+$  state of the  $^{24}\text{O}$  core, or by coupling of a  $p_{3/2}$  proton hole to the  $2^+$  or  $1^+$  state in the  $^{24}\text{O}$  core. The ground state of  $^{24}\text{O}$  has very little to no overlap with these configurations in  $^{23}\text{N}$ .

The spectroscopic overlaps  $C^2S$  between  $^{23}\text{N}$  and  $^{24}\text{O}$  were calculated using the WBP and WBT Hamiltonians in NUSHELLX [28] and are summarized in Table I. The largest overlap is with the ground state of  $^{23}\text{N}$ , which is bound and was not within the acceptance of the sweeper magnet in this

TABLE I. Spectroscopic overlaps between various  $J^\pi$  in  $^{23}\text{N}$  and the ground state of  $^{24}\text{O}$ , calculated using the WBP and WBT interactions [25].

$J^\pi$	WBP		WBT	
	$E_{\text{calc}}$ (MeV)	$\langle ^{23}\text{N}   ^{24}\text{O} \rangle$ $C^2S$	$E_{\text{calc}}$ (MeV)	$\langle ^{23}\text{N}   ^{24}\text{O} \rangle$ $C^2S$
$1/2_1^-$	0	1.9328	0	1.9529
$1/2_2^-$	4.961	0.0025	5.257	0
$\sum C^2S$		1.9578		1.9529
$3/2_1^-$	3.610	1.4645	3.610	0.6893
$3/2_2^-$	4.525	0.6480	4.764	1.0483
$3/2_3^-$	5.215	0.1682	5.471	0.0944
$3/2_4^-$	6.989	1.4324	6.693	1.8889
$\sum C^2S$		3.7130		3.7209

experiment. The next strongest overlaps are for the  $3/2^-$  states where the single-particle strength is fragmented. Given that the overlap for the first  $1/2^-$  excited state is very small, the most likely candidate for the spin-parity of the observed state(s) is  $3/2^-$ .

It is important to note that  $^{22}\text{N}$  has two bound excited states, one at 183 keV, and another at 1017 keV [22]. Although the spin-parities of these states are unknown, the tentative assignments of the ground, first, and second excited states are  $0^-$ ,  $1^-$ , and  $2^-$ , respectively. Thus, the observed peaks in the two-body decay energy could correspond to transitions to the  $2^-$  excited state of  $^{22}\text{N}$  instead of the ground state or the first excited  $1^-$  state. Although there are neutron-unbound states in  $^{22}\text{N}$  that  $^{23}\text{N}$  could decay to, the selection of  $^{22}\text{N}$  in the sweeper eliminates any contributions from these branches in the two-body spectrum of  $^{23}\text{N}$ .

As it is not possible to discern between any number of degeneracies or level orderings that could produce the observed spectrum without measuring the emitted  $\gamma$  rays, one has to rely on theoretical calculations. For this reason, the data are interpreted and fit within the context of the shell-model predictions.

Of the interactions considered here, none predict a state near threshold (see Fig. 2). The lowest  $3/2^-$  state is predicted to be at approximately 1 MeV above  $S_n$ , with the second  $3/2^-$  being about an MeV higher. The 100 keV peak then does not correspond to a decay to the ground state but rather a transition to the  $2^-$  state in  $^{22}\text{N}$ , while the  $E_2 \sim 1$  MeV peak is comprised of transitions to both the first-excited and ground state of  $^{22}\text{N}$ . While there are three possible final states, the splitting between the ground and first-excited state cannot be resolved due to the experimental resolution for decay energies above 1 MeV. For

this reason, the  $0^-$  and  $1^-$  states are treated as a single state at their average energy. Since the spacing between the two  $3/2^-$  states is expected to be about an MeV, another state was assumed to be around  $\sim 2$  MeV. In addition, because the final states in  $^{22}\text{N}$  are only tentatively known, the  $\ell$  values are chosen to be consistent with the interpretation.

The assumption of a second excited state is qualitatively supported by the data, as the high-energy tail cannot be described without excessive widths. In order to fit the spectrum with a single two-channel Breit-Wigner, it is necessary for the 1 MeV peak to have  $\ell = 2$  and a width of  $\Gamma \sim 1.5$  MeV. In this scenario, it is also necessary for the 100 keV branch to be  $\ell = 0$  as the relative intensity of the peaks is driven by the partial widths. The cross section for  $\ell = 2$  drops rapidly as  $E_{\text{decay}}$  approaches zero and the 100 keV peak cannot be  $\ell = 2$  in the presence of another broad channel unless it has an even larger width.

The spectrum can also not be described with both channels being  $\ell = 0$ , because the widths are coupled and the penetrability for  $\ell = 0$  is constant. Thus, if the 1 MeV channel is made excessively broad so too is the 100 keV branch and the fit fails to describe the data.

The single-particle decay width for the decay to the ground state is 200 keV for  $\ell = 2$ . Examining the spectroscopic factors in Table I, we note that the  $3/2^-$  single-particle strength is fragmented indicating that these states are mixed in their neutron configurations. Thus one would expect widths less than the single-particle width, and so the solution with a single state is neglected due to the large necessary width. The data are fit with two-channel Breit-Wigners resulting from two  $3/2^-$  states separated by approximately 1 MeV.

Since the branching ratios are not constrained without the knowledge of the  $\gamma$ -ray decays in  $^{22}\text{N}$ , there are too many free parameters to uniquely describe the data. Therefore a set of narrow widths was chosen to reduce the parameter space. These widths are  $\Gamma_i = 150$  keV for the low-energy branches of the two states ( $\ell = 0$ ) and 400 keV ( $\ell = 0$ ) and 300 keV ( $\ell = 2$ ) for the high-energy branch of the first and second  $3/2^-$  states, respectively.

The energies of the two  $3/2^-$  are then minimized simultaneously after fixing the partial widths. In addition, the energy of each branch is required to be consistent during the minimization. The best-fit energies for the two  $3/2^-$  states are  $E_{\text{decay}} = 1070 \pm 100$  keV, and  $E_{\text{decay}} = 2500_{-700}^{+500}$  keV. The errors in the fit parameters are approximate due to the fixed partial widths. They are purely statistical and are determined by the  $1\sigma$  limit in the  $\chi^2$  minimization. Accounting for the separation energy places the first excited  $3/2^-$  at  $E_x = 3530 \pm 100$  (stat)  $\pm 400$  (sys) keV.

At present the uncertainties are too large to uniquely determine the contributions from the possible branchings two  $3/2^-$  states would produce. In order to completely disentangle the spectrum, one would need to measure the emitted  $\gamma$  rays in a triple-coincidence measurement ( $n + \gamma + ^{22}\text{N}$ ).

#### IV. DISCUSSION

The present measurement alone is not sufficient to fully determine the size of the  $N = 16$  shell gap in  $^{23}\text{N}$ . In  $^{24}\text{O}$

the  $N = 16$  shell gap was calculated by taking the  $(2J + 1)$  weighted average of the  $1^+$  and  $2^+$  excited states, as they are composed of  $1p-1h$  excitations above the  $^{24}\text{O}$  ground state [4]. Similarly, the same can be done in  $^{23}\text{N}$ , but one needs to take into account four states as the  $2^+$  and  $1^+$  configuration of neutrons,  $(\nu 1s_{1/2})^1 \otimes (\nu 0d_{3/2})^1$ , can couple with the unpaired  $\pi 0p_{1/2}$  proton to give  $(5/2^-, 3/2^-)$  and  $(3/2^-, 1/2^-)$ , respectively. The situation is further complicated by the fact that the  $1p-1h$  neutron configuration in  $^{23}\text{N}$  will mix with the  $\pi 0p_{3/2}$  hole, lowering its energy.

In the WBP, WBT, WBTM, and WBM interactions, the lowest  $3/2^-$  state in  $^{23}\text{N}$  is indeed a mixture, with the occupation numbers giving a significant proton hole in the  $\pi p_{1/2}$  and  $\pi p_{3/2}$  orbitals, and a  $(\nu 1s_{1/2})^1 \otimes (\nu 0d_{3/2})^1$  configuration of neutrons. One may write the wave function for the  $3/2^-$  state as

$$|^{23}\text{N}\rangle_{3/2^-} = \alpha p_{3/2}^{-1} \otimes |^{24}\text{O}\rangle_{\text{g.s.}} + \beta p_{1/2}^{-1} \otimes |^{24}\text{O}\rangle_{2^+} + \gamma p_{1/2}^{-1} \otimes |^{24}\text{O}\rangle_{1^+},$$

where  $\alpha$ ,  $\beta$ , and  $\gamma$  are coefficients constrained by the normalization  $\alpha^2 + \beta^2 + \gamma^2 = 1$ . According to the WBP calculation, the pure  $\pi p_{3/2}^{-1}$  configuration comprises of roughly 37% of the total wave function ( $\alpha \sim 1/\sqrt{3}$ ), with the remaining amplitude shared equally between the  $2^+$  and  $1^+$  configurations.

Thus the energy of the lowest  $3/2^-$  state depends on both the  $N = 16$  shell gap and the energy of the  $\pi 0p_{3/2}^{-1}$  hole, which is dictated by the spin-orbit splitting. The splitting between the  $d_{3/2}-s_{1/2}$  and  $p_{1/2}-p_{3/2}$  orbitals can be altered within NUSHELLX to study this dependence.

Let  $\Delta$  denote the change in energy for either the  $d_{3/2}$  or  $p_{1/2}$  orbital for both protons and neutrons from their initial values in the WBP calculation, using the same model-space restrictions as before. Figure 3 shows the energy of the lowest  $3/2^-$  state as

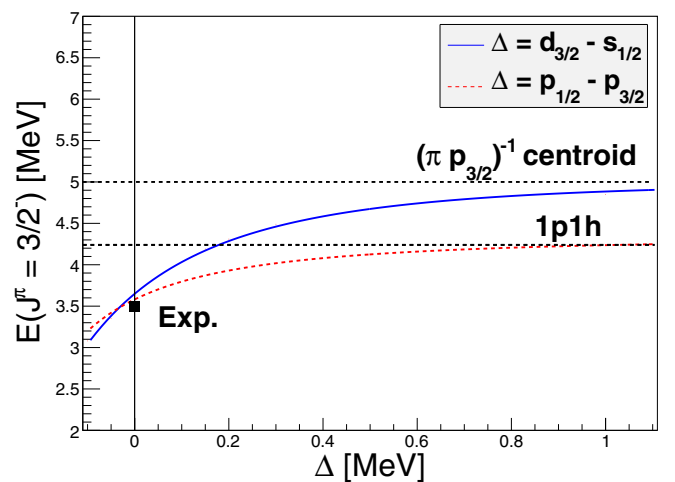


FIG. 3. Energy dependence of the first-excited  $3/2^-$  state on the shift,  $\Delta$ , on the energy of the  $d_{3/2}$  orbital (solid-blue line) or  $p_{1/2}$  orbit (dashed-red line). The dotted black lines denote the energies of the pure  $1p-1h$  or  $\pi p_{3/2}^{-1}$  configurations in the initial calculation ( $\Delta = 0$ ). The experimental energy determined in this work is denoted by the black square.

a function of either the  $N = 16$  shell gap (solid-blue line) or the spin-orbit splitting (dotted-red line). By increasing the energy of the  $d_{3/2}$  or  $p_{1/2}$  orbitals independently, the mixing between the configurations is reduced until they are separated at the asymptotes. In the case of the  $d_{3/2}$  orbit, increasing the  $N = 16$  shell gap causes the  $1p-1h$  configuration to be prohibitively costly in energy thus the  $3/2^-$  state is comprised entirely of the  $\pi p_{3/2}^{-1}$  hole. Likewise, increasing the spin-orbit splitting causes the promotion of a particle from the  $\pi p_{3/2}$  to the  $\pi p_{1/2}$  to be too energetic, and the lower energy configuration is instead the  $1p-1h$  configuration across the  $N = 16$  shell gap.

Evidence for the size of the  $N = 16$  shell gap in  $^{24}\text{O}$  can be deduced from the energy of the first excited  $2^+$  state as shown in Figure 4 of Ref. [4]. In order to calculate the equivalent energy in  $^{23}\text{N}$  one has to take the  $(2J + 1)$  weighted average of the first  $3/2^-$  and  $5/2^-$  states. All Hamiltonians considered in Fig. 2 predict these two states to be nearly degenerate, thus the excitation energy of the  $3/2^-$  measured in the present experiment can be used to estimate the equivalent  $2^+$  energy.

The most recent ENSDF evaluation lists the excitation energy of the first  $2^+$  in  $^{24}\text{O}$  as 4.79(11) MeV [29], corresponding to the weighted average of 4.82(11) [4] and 4.75(14) [5]. A more recent measurement of 4.70(15) MeV [30] agrees with this evaluation.

The present value of the excitation energy of about 3.5 MeV for the  $3/2^-$  state in  $^{23}\text{N}$  is 1.3 MeV lower than the  $2^+$  state in  $^{24}\text{O}$ . In the limit of no mixing from the  $p_{3/2}^{-1}$  hole configuration,  $[\Delta(p_{1/2}) \sim 1]$ , the energy of the lowest  $3/2^-$  increases from 3.61 MeV to 4.24 MeV which is 500 keV lower than the excitation of the  $2^+$  in  $^{24}\text{O}$ . The  $N = 16$  shell gap, or the  $(2J + 1)$  average of the four lowest states in the  $1p-1h$  multiplet, is around 4.53 MeV when the contributions from the  $p_{3/2}^{-1}$  configuration are removed. This value is 300–400 keV lower than in  $^{24}\text{O}$  where this average was found to be 4.95(16) MeV [4], thus the shell gap in  $^{23}\text{N}$  is comparable to  $^{24}\text{O}$ . The shift in the effective  $2^+$  energy is largely due to the coupling to the  $p_{3/2}$  hole. In order to confirm this experimentally the excitation energy of the  $5/2^-$  state in  $^{23}\text{N}$  should be measured.

## V. CONCLUSIONS

Neutron unbound excited states in  $^{23}\text{N}$  were populated via proton knockout from an  $^{24}\text{O}$  beam on a deuterium target. The two-body decay energy of  $^{23}\text{N}$  displays two prominent peaks at  $E_1 \sim 100$  keV and  $E_2 \sim 1$  MeV. Because the daughter nuclide  $^{22}\text{N}$  has two bound excited states, it is not possible to distinguish between degeneracies or multiple level schemes that may produce the observed energy differences in the two-body spectrum of  $^{23}\text{N}$ . A triple coincidence experiment detecting the  $^{22}\text{N}$  fragments, neutrons and  $\gamma$  rays is necessary to measure the branchings to the different final states.

The data are consistent with several shell model interactions which predict a  $3/2^-$  state at  $\sim 1$  MeV and  $\sim 2$  MeV above  $S_n$  in  $^{23}\text{N}$ . Similar to the first excited  $2^+$  state in  $^{24}\text{O}$ , the first of these two  $3/2^-$  states can be used to estimate the  $N = 16$  shell gap. Its excitation energy of about 3.5 MeV is significantly lower than the  $^{24}\text{O}$   $2^+$  state at 4.8 MeV, however this reduction is largely due to configuration mixing with the  $\pi p_{3/2}^{-1}$  hole, thus indicating only a slight a reduction of the  $N = 16$  gap in nitrogen.

Finally, in order to compare these data directly it is necessary to measure the first excited  $5/2^-$  state in  $^{23}\text{N}$ . A future experiment designed to populate this state, for example inelastic excitation of  $^{23}\text{N}$ , would be valuable. In addition, the distribution of single-particle strength for the  $3/2^-$  will be vital to determining the  $\pi p_{3/2}^{-1}$  centroid experimentally and further understanding the mixing between the  $1p1h$  and  $\pi p_{3/2}^{-1}$  configurations.

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